## Effect of Input Resistance Voltage-Dependency on DC Estimate of Membrane Capacitance in Cardiac Myocytes

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ABSTRACT The measure of membrane capacitance  $(C_{\rm m})$  in cardiac myocytes is of primary importance as an index of their size in physiological and pathological conditions, and for the understanding of their excitability. Although a plethora of very accurate methods has been developed to access  $C_{\rm m}$  value in single cells, cardiac electrophysiologists still use, in the majority of laboratories, classical direct current techniques as they have been established in the early days of cardiac cellular electrophysiology. These techniques are based on the assumption that cardiac membrane resistance  $(R_{\rm m})$  is constant, or changes negligibly, in a narrow potential range around resting potential. Using patch-clamp whole-cell recordings, both in current-clamp and voltage-clamp conditions, and numerical simulations, we document here the voltage-dependency of  $R_{\rm m}$ , up to -45% of its resting value for 10-mV hyperpolarization, in resting rat ventricular myocytes. We show how this dependency makes classical protocols to misestimate  $C_{\rm m}$  in a voltage-dependent manner (up to 20% errors), which can dramatically affect  $C_{\rm m}$ -based calculations on cell size and on intracellular ion dynamics. We develop a simple mechanistic model to fit experimental data and obtain voltage-independent estimates of  $C_{\rm m}$ , and we show that accurate estimates can also be extrapolated from the classical approach.

### INTRODUCTION

The value of membrane capacitance  $(C_{\rm m})$  is a measure of how much charge is needed to displace cell polarization, how fast cell membrane passively responds to current/voltage changes, and how large is the membrane surface area.  $C_{\rm m}$ and input resistance  $(R_{\rm m})$  of excitable cells are usually referred to as passive electrical properties and derived referring to an equivalent circuit, parallel combination of the two electrical elements. Microelectrode and patch-clamp techniques which have been developed, under current-clamp (CC) and voltage-clamp (VC) conditions, to solve this parallel RC combination to calculate  $C_{\rm m}$  (1,2), can be grouped in two categories: the alternating current (AC) and the direct current (DC) methods. Very accurate estimates of  $C_{\rm m}$  are achieved using AC methods, by means of single or multiple sinusoidal command voltages, used to clamp the cell with two-phase lock-in amplifiers (3,4). Square-wave stimulations are also employed and analyzed in the frequency domain (5), and ramp command voltage protocols have been recently improved (6) and applied to cardiac myocytes (7,8). These techniques have been originally established and largely employed mainly to study changes in membrane area during exocytosis and endocytosis (3,9,10), but they are still too technically demanding for a more general use (6) like the estimate of cell size in cardiac preparations.

The measure of specific  $C_{\rm m}$  ( $\mu$ F/cm<sup>2</sup>) in cardiac tissue and, since the introduction of enzymatic isolation procedures, of  $C_{\rm m}$  (pF) in single cardiac myocytes, has been pursued from the early days of cardiac electrophysiology (11–13), given the pivotal role of this parameter in cardiac excitability and the

physiopathological interest in monitoring cell size in the heart. Systematic errors in the measure of  $C_{\rm m}$  will lead, for example, to erroneous evaluation of cardiomyocytes remodeling in studies where this parameter is measured in hypertrophied hearts (7,14,15), failing hearts (16), dilated cardiomyopathy (17), diabetes (18), and myocardial infarction (19). Such errors will also affect studies on intercellular electrotonic interactions (20–22) where  $C_{\rm m}$  plays a primary role in determining source-sink properties of interacting cells. Finally, they will affect those studies where  $C_{\rm m}$  is measured to normalize transsarcolemmal ion currents and fluxes through carriers to cell surface and, indirectly, to cell volume (23).

Definitely the more common tool adopted by cardiac electrophysiologists to measure  $C_{\rm m}$  remains the use of timedomain DC methods, where constant current (or voltage) steps are imposed to the cell membrane and the study of the resulting voltage (or current) displacements is performed in terms of mono-exponential functions (1), a procedure which, as recently pointed out (6), has not been modified substantially since its introduction 30 years ago (24). This approach is based on the assumption that  $C_{\rm m}$  is constant for a given cell, and that  $R_{\rm m}$  is fairly constant over membrane potential  $(V_{\rm m})$  changes (1), at least in the voltage range of application of the mentioned protocols. Since  $R_{\rm m}$  changes have been documented around the resting potential  $(V_{\rm r})$  (cited below), the second assumption is actually that these changes are negligible with respect to  $C_{\rm m}$  estimate.

The fact that  $R_{\rm m}$  changes during the cardiac action potential follows directly from the Hodgkin-Huxley theory of membrane excitability, has been described by Weidmann in early days (25), and recently measured in guinea pig ventricular myocytes (22). In addition, Weidmann, by means

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of constant current injections into cardiac fibers, noticed that  $R_{\rm m}$  continuously decreased, starting from threshold  $V_{\rm m}$  toward rest and for increasingly hyperpolarizing current injections. The decrease of  $R_{\rm m}$  as membrane potential hyperpolarizes with respect to threshold potential, is accounted for in cardiac myocytes mainly by inward rectification of  $I_{\rm K1}$  (26,27) and has already been measured in isolated rat ventricular myocytes (13,28).

In the present work, we show that  $R_{\rm m}$  voltage-changes around  $V_{\rm r}$  are indeed not negligible when standard CC/VC protocols are used to calculate  $C_{\rm m}$ , which therefore results to be voltage-dependent as well. To this end, we measure the  $R_{\rm m}(V_{\rm m})$  function around  $V_{\rm r}$  and incorporate it in a mechanistic RC equivalent model, which better resembles membrane passive electrical properties. The numerical solution of such circuit allows accurate estimates of  $C_{\rm m}$  which do not depend on voltage. We suggest that  $I_{K1}$  rectification, as the main responsible for the input resistance voltage dependency, is also the primary source for the error in  $C_{\rm m}$  estimate through the classical approach. This study, performed in turn, on real isolated rat ventricular myocytes, on five different mathematical models of the cardiac action potential, and on a simple RC mathematical model, also suggests a simplified procedure that allows to derive accurate estimates of  $C_{\rm m}$  with the classical constant CC and VC protocols.

### **MATERIALS AND METHODS**

### **Cell isolation**

Single cells were obtained by enzymatic dispersion of adult (6 months, 400–500 g) male Wistar rat left ventricles. After thoracotomy, the heart was rapidly removed, mounted on a Langendorff apparatus, and perfused at  $37^{\circ} C$  with the following sequence of solutions:  $\text{Ca}^{2^{+}}\text{-free}$  (control, no added calcium) Tyrode solution for 5 min to remove the blood, low- $\text{Ca}^{2^{+}}$  (0.1 mM) solution containing 1 mg/ml type 2 collagenase (Worthington, Lakewood, NJ) and 0.1 mg/ml type XIV protease (Sigma Aldrich, Milan, Italy) for 20 min, and enzyme-free low- $\text{Ca}^{2^{+}}$  solution for 5 min. The left ventricle was then minced and shaken for 10 min in the low- $\text{Ca}^{2^{+}}$  solution. Myocytes were stored at room temperature in the control solution with 0.5 mM  $\text{Ca}^{2^{+}}$ . All experiments were performed within 2–8 h after isolation. All myocytes used in this study had well-defined striations and did not spontaneously contract.

### **Solutions**

Isolation solution contained 126 mM NaCl, 22 mM dextrose, 5.0 mM MgCl<sub>2</sub>, 4.4 mM KCl, 20 mM taurine, 5 mM creatine, 5 mM Na pyruvate, 1 mM NaH<sub>2</sub>PO4, and 24 mM HEPES (pH = 7.4 adjusted with NaOH). The solution was gassed with 100% O<sub>2</sub>. Control solution for cell bathing during experiments contained 126 mM NaCl, 11 mM dextrose, 5.4 mM KCl, 1.0 mM MgCl<sub>2</sub>, 1.08 mM CaCl<sub>2</sub>, and 24 mM HEPES (pH-adjusted to 7.4 with NaOH). The pipette filling solution contained 113 mM KCl, 10 mM NaCl, 5.5 mM dextrose, 5 mM K<sub>2</sub>ATP, 0.5 mM MgCl<sub>2</sub>, and 10 mM HEPES (pH-adjusted to 7.1 with KOH). A drop of cells was placed in the experimental chamber (~2.5 ml) and superfused by gravity at a flow rate of ~2 ml/min. The temperature of the solutions in the cell bath was 37°C.

### **Electrical recordings**

Suction pipettes were made from borosilicate capillary tubing (Harvard Apparatus, Edenbridge, United Kingdom) and had a resistance, when filled,

of 2–4  $M\Omega$ . Transmembrane potential and current (*i*) were recorded by means of an Axoclamp 2B amplifier (Axon Instruments, Union City, CA) adopting the whole-cell configuration of the patch-clamp technique.

### Classical DC protocols to measure $C_{\rm m}$

Here we summarize time-domain DC methods for the estimate of  $C_{\rm m}$  which have been adopted and criticized in this study. For the sake of clarity, we will consider the resting membrane potential  $V_{\rm r}$  set to zero.

### CC approach

Cells were held in whole-cell configuration (amplifier in Bridge mode) and injected at a frequency of 2 Hz, with 200-ms constant current pulses  $(i_p)$  usually starting from -0.260 nA and incrementing with 5-pA steps up to 0.235 nA. Subthreshold voltage deflections were sampled at 5 kHz, digitized (Digidata 1200 Series Interface, Axon Instruments, Union City, CA), and best fitted with mono-exponential functions (Kaleidagraph, Synergy Software, Reading, PA) as solutions

$$V_{\rm m}(t) = i_{\rm p} \times R_{\rm m} \times (1 - e^{-t/\tau}); \quad V_{\rm m}(0) = V_{\rm r} = 0; \quad \tau = R_{\rm m} \times C_{\rm m}$$
(1)

of the equation

$$\dot{V}_{\rm m}(t) = \frac{1}{C_{\rm m}} \times \left(i_{\rm p} - \frac{V_{\rm m}(t)}{R_{\rm m}}\right),\tag{2}$$

relative to the linear equivalent parallel RC circuit. It is straightforward to derive the plateau value of  $V_{\rm m}(t)$  as  $V_{\infty}=i_{\rm p}\times R_{\rm m}$ . The description does not include any additional series pipette resistance  $R_{\rm s}$ , which was electrically compensated with bridge balance. Passive electrical properties  $R_{\rm m}$  and  $C_{\rm m}$  were derived as best-fitting parameters of experimental voltage traces with Eq. 1.

### VC approach, curve fit

To minimize filtering effects due to pipette capacitance, pipettes tips were coated with a hydrophobic compound (Sylgard, Dow Corning, Midland, MI) and the cell bath was maintained at a low level (1 mm). Protocol features were analogous to current clamp; with the amplifier in discontinuous single-electrode voltage-clamp mode, cells were initially clamped at their  $V_{\rm r}$  and then stepped with 40-ms constant voltage-clamps ( $V_{\rm c}$ ) usually starting from  $V_{\rm r}-20~{\rm mV}$  and incrementing with 1-mV steps up to  $V_{\rm r}+15~{\rm mV}$ . Current traces were best fitted with mono-exponentials as linear functions

$$i(t) = (V_{\rm c} - V_{\rm m}(t))/R_{\rm s}$$
 (3)

of the solutions

$$V_{\rm m}(t) = \frac{R_{\rm p}}{R_{\rm s}} \times V_{\rm c} \times (1 - e^{-t/(R_{\rm p} \times C_{\rm m})});$$

$$V_{\rm m}(0) = V_{\rm r} = 0; \quad R_{\rm p} = \frac{R_{\rm s} \times R_{\rm m}}{R_{\rm s} + R_{\rm m}}$$

$$(4)$$

of the equation

$$\dot{V}_{\rm m}(t) = \frac{1}{C_{\rm m}} \times \left( \frac{V_{\rm c} - V_{\rm m}(t)}{R_{\rm s}} - \frac{V_{\rm m}(t)}{R_{\rm m}} \right),$$
 (5)

relative to the linear equivalent parallel RC circuit in series with an additional access resistance  $R_{\rm s}$ .  $R_{\rm m}$ ,  $C_{\rm m}$ , and  $R_{\rm s}$  were derived as best fitting parameters. Membrane potential  $V_{\infty}$ , corresponding to the plateau value of the current ( $i_{\infty} = V_{\rm c} / (R_{\rm m} + R_{\rm s})$ ), was derived as  $V_{\rm c} - i_{\infty} \times R_{\rm s}$ , being the additional  $R_{\rm s}$  uncompensated during the protocol.

In the following discussion, we will use the notation  $\Delta V_{\rm m} = V_{\infty} - V_{\rm r} = V_{\infty}$  for the steady-state value reached by  $V_{\rm m}$  during CC and VC protocols.

### VC approach, area of the transient

An alternative VC method to measure  $C_{\rm m}$ , to which we refer in this work, is to measure the charge under the current transient and divide it by the  $\Delta V = V_{\rm c} - V_{\rm r}$ . This is often approximated as

$$C_{\rm m} = \frac{Q}{\Lambda V},\tag{6}$$

where Q is the area under the current transient and above  $i_{\infty}$ . Recently a better approximation for this is adopted (16) as

$$C_{\rm m} = \frac{Q + i_{\infty} \times \tau}{\Lambda V},\tag{7}$$

where Q is the area under the current transient and above  $i_{\infty}$  and  $i_{\infty} \times \tau$  is an approximation for the area under  $i_{\infty}$  and above the exponential resistive component of the current response.

### Computer simulations

The electrical properties of single resting cardiomyocytes were simulated, in turn, using membrane equations from the mathematical models listed in Table 1, or solving Eq. 2 and Eq. 5 for a simple RC circuit including a series resistance  $R_{\rm s}$ , which was set to zero in CC simulations. Equations were numerically solved using an adaptive Euler method for the LR91 model, and a fifth-order Runge-Kutta method for PD01 model and for the RC circuit. Simulations on the LR94, PB01, and RM00 were performed on the Cell Electrophysiology Simulation Environment (CESE Version 1.3.4, available on http://cese.sourceforge.net). All simulations were performed on a Pentium IV processor and codes for LR91, PD01, and for the RC circuit implemented in MatLab language (The MathWorks, Natick, MA).

### **Statistics**

Results are presented as mean  $\pm$  SE. Statistical analysis was performed using the unpaired Student's *t*-test with SPSS software (SPSS, Chicago, IL). Statistical significance was set at P < 0.05.

### **RESULTS**

### Estimate of an input resistance voltage-function

The membrane input resistance  $(R_{\rm m})$  of single rat ventricular myocytes was measured within  $\sim \pm 10$  mV around resting potential  $(V_{\rm r})$  through CC and VC protocols (see Materials and Methods). Fig. 1 A shows voltage deflections from a CC protocol and the function  $R_{\rm m}(\Delta V_{\rm m})$  well fitted by a parabola  $c_0+c_1\times\Delta V_{\rm m}+c_2\times\Delta V_{\rm m}^2$  with  $c_0=58.35, c_1=3.64$ , and

TABLE 1 The different mathematical models tested in their subthreshold electrical properties

Cell type	Reference	Abbreviation
Mammalian ventricular	Luo and Rudy (42)	LR91
Guinea pig ventricular	Luo and Rudy (43)	LR94
Rabbit ventricular	Puglisi and Bers (44)	PB01
Rat ventricular	Pandit et al. (30)	PD01
Canine atrial	Ramirez et al. (45)	RM00

 $c_2=0.14$ . The same analysis performed on 12 myocytes gave an average parabolic fitting of  $c_0=55.99\pm3.67, c_1=2.37\pm0.25$ , and  $c_2=0.06\pm0.01$ . Current traces from a VC protocol are reported in Fig. 1 B with the function  $R_{\rm m}(\Delta V_{\rm m})$ , which is similar to the one measured in CC, and well fitted by a parabola with  $c_0=54.22, c_1=4.51$ , and  $c_2=0.12$ . The same analysis performed on 12 myocytes gave an average fitting of  $c_0=58.76\pm6.95, c_1=5.22\pm0.59$ , and  $c_2=0.15\pm0.02$ . When the two protocols were numerically simulated on a LR91 model, they returned a qualitatively analogous function  $R_{\rm m}(\Delta V_{\rm m})$ , well fitted by a parabola with  $c_0=21.71, c_1=1.10$ , and  $c_2=0.027$ . Similar  $R_{\rm m}(\Delta V_{\rm m})$  behavior was found in all five mathematical models employed (see below).

### Estimate of the capacitance for a non-Ohmic RC

A constant  $R_{\rm m}$  around resting potential  $V_{\rm r}$  (which we will refer to as the Ohmic assumption in the following discussion) is required in classical DC measurements of  $C_{\rm m}$ . If, as shown above,  $R_{\rm m}$  changes up to 30–50 M $\Omega$  within  $\pm 10$  mV around  $V_{\rm r}$ , the solution of a non-Ohmic circuit that includes the  $R_{\rm m}(\Delta V_{\rm m})$  function (which we will call the non-Ohmic assumption) should be more appropriate.

In Fig. 2 we show examples in which  $C_{\rm m}$  was calculated (see Materials and Methods) by mono-exponential fittings of the voltage/current traces reported in Fig. 1. The measured  $C_{\rm m}$  varies with  $\Delta V_{\rm m}$ , decreasing with membrane polarization. The same analysis performed on seven myocytes led to  $C_{\rm m}$  changes, as measured from a linear fitting for  $-10\,{\rm mV}$  $\Delta V_{\rm m}$  < 0 mV, of 2.95  $\pm$  0.74 pF/mV in CC and 1.35  $\pm$  0.54 pF/mV in VC. Analogous results are shown, for example, on the more general LR91 model. Analyzing a non-Ohmic RC as if it was Ohmic clearly leads to an error in  $C_{\rm m}$  estimate, which increases with the displacement of membrane potential from  $V_r$ , doing more so in CC than in VC. The CC protocol was applied also on the other mathematical models listed in Table 1, and results reported in Fig. 3. In the lower panel of the same figure, the relationship between the relative error in  $C_{\rm m}$  estimate and  $R_{\rm m}$  rectification is also reported for the five mathematical models and for the experimental data. To better isolate this effect, we solved two simple mathematical models of a resting myocyte in wholecell configuration, which included only  $R_s$ ,  $C_m$ , and  $R_m$  (Fig. 4).  $R_{\rm m}$  was kept constant in a first case (Fig. 4 A) and voltagedependent in a second case (Fig. 4 B). Fig. 4 A shows the symmetrical behavior (with respect to the resting potential/ current) of voltage and current traces obtained when the Ohmic circuit (Fig. 4 A) was solved, in turn, in CC and VC conditions. When the constant  $R_{\rm m}$  of the circuit was replaced (as in Fig. 4 B) with an experimental  $R_{\rm m}(\Delta V_{\rm m})$  function of the type shown in Fig. 1, the voltage and current deflections lost their symmetry and appeared more like those measured in real cells. Traces were all analyzed in terms of monoexponential fittings (see Materials and Methods), assuming each time, for  $R_{\rm m}$ , the constant value measured at plateau,

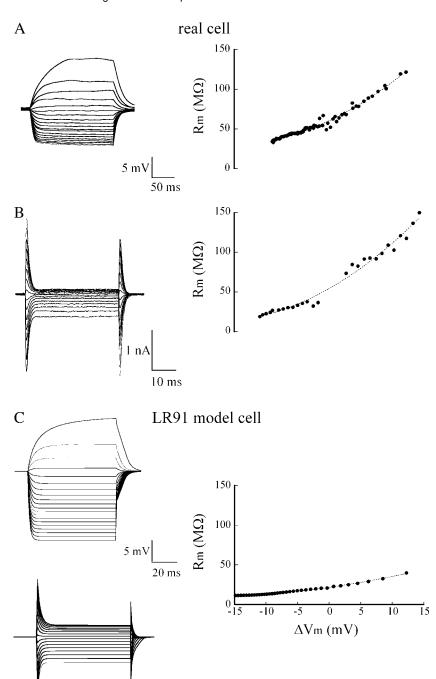


FIGURE 1 Measure of  $R_{\rm m}$  voltage-dependency. Left column: (A) voltage deflections from a CC protocol on a rat myocyte. Only one in every four traces is shown for clarity. (B) Current traces from a VC protocol on a different myocyte. Only one in every second trace is shown. (C) Analogous CC and VC protocols simulated on the LR91 model ( $R_{\rm s}=5~{\rm M}\Omega$  in VC). Right column:  $R_{\rm m}$ , calculated from plateau values of each voltage and current trace, is reported (solid circles) as a function of  $\Delta V_{\rm m}$ , fitted by parabolic functions (dotted lines).

and  $C_{\rm m}$  values derived and reported as solid circles in Fig. 4 C. The Ohmic assumption, in the case of a physiologically non-Ohmic RC circuit, leads to an error in the estimate of  $C_{\rm m}$  which qualitatively reproduces what we found in real myocytes and in the mathematical model cells (Fig. 2 and Fig. 3), with  $C_{\rm m}$  varying with a sigmoidal-law around the resting potential.

In Fig. 5 two additional examples of  $C_{\rm m}$  derived through mono-exponential fittings in two real ventricular myocytes are shown. In addition, the  $R_{\rm m}(\Delta V_{\rm m})$  parabolic functions, derived from both cells, were, in turn, included in a math-

ematical non-Ohmic model equivalent to the one in Fig. 4 B. The value  $R_{\rm s}$  was also derived from the VC protocols, and was included in the model. Each voltage and current trace was then fitted with numerical solutions of the non-Ohmic form of Eq. 2 and Eq. 5 including the experimentally derived  $R_{\rm m}(\Delta V_{\rm m})$ , to obtain new estimates of  $C_{\rm m}$  (see Appendix for details on the algorithm), also reported in the figures. Whereas  $C_{\rm m}$ , measured in the Ohmic assumption, is voltage-dependent and varies  $\sim$ 2.1 pF/mV in CC and 1.9 pF/mV in VC, the values derived upon considering the non-Ohmic assumption were fairly constant within the voltage range

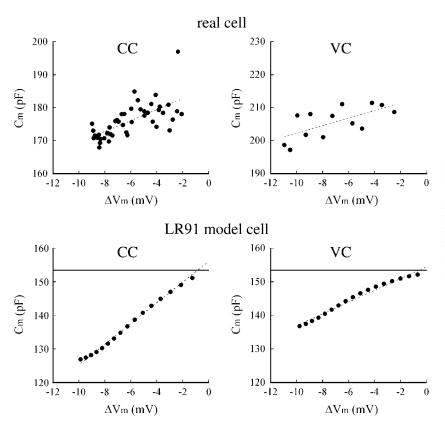


FIGURE 2 Estimated  $C_{\rm m}$  as a function of  $V_{\rm m}$  displacement from  $V_{\rm r}$ . (*Top*) Each solid circle represents a DC estimate of  $C_{\rm m}$  from experimental traces of Fig. 1, A and B. (*Bottom*) Same for the traces from the LR91 model in Fig. 1 C, where  $C_{\rm m}$  was set to 153.44 pF (horizontal lines) on the basis of the geometrical considerations of Luo and Rudy (43). Dotted lines in each panel represent linear fittings of the experimental data, 1.6, 1.1, 3.1, and 1.7 pF/mV, respectively.

under study, being 128.4  $\pm$  0.6 pF in CC and 150.2  $\pm$  1.1 pF in VC. Same result (voltage-independent estimates of  $C_{\rm m}$ ) was obtained when all five mathematical model cells were studied within the non-Ohmic assumption (not shown). For an additional control, we numerically simulated the CC and VC real experiment on two non-Ohmic model circuits like the one in Fig. 4 B, including, respectively, the non-Ohmically calculated two mean values of the  $C_{\rm m}$ , the  $R_{\rm m}(\Delta V_{\rm m})$  functions and  $R_{\rm s}$ . When we fitted the numerically integrated voltage and current traces with mono-exponentials, we found a continuous  $C_{\rm m}(\Delta V_{\rm m})$  function that well fits the  $C_{\rm m}$  values Ohmically derived from experimental data. The same type of analysis was performed with analogous results on seven current-clamped and seven voltage-clamped ventricular myocytes where  $C_{\rm m}$  values from different cells were normalized for comparison to the constant value found each time with non-Ohmic assumption, which was set to 1. Average error in normalized  $C_{\rm m}$  estimate was 0.0189 mV<sup>-1</sup> in CC and 0.0097 mV<sup>-1</sup> in VC. Analogous results were obtained when  $C_{\rm m}$  was measured in the LR91 model (Fig. 6). In summary, when, instead of using mono-exponential fittings, we solved a mechanistic model including the  $R_{\rm m}$  $(\Delta V_{\rm m})$  derived from the simulated traces, we were able to measure, at least in a 10–15-mV range below  $V_r$ , a value of  $C_{\rm m}$  that tightly resembles the actual one.

Another way, used in early works, to study the time course of voltage deflections in constant step-CC experiments, was to plot the logarithm of the voltage displacement as a function of time (13,1), which should result in a straight line in the case of mono-exponential rise. In Fig. 7 A we show, in a real cell, the time course of a voltage displacement from a CC protocol, together with the time course of its logarithm, respectively fitted with a mono-exponential and a straight line ( $C_{\rm m}$  derived as 152 pF). Although other traces from the same experiment revealed a 10-M $\Omega$  difference between  $R_{\rm m}$  measured at  $V_{\infty}=-8$  mV and  $V_{\infty}=-4$  mV (Fig. 7, arrows), which in turn resulted in a 20-pF difference in the  $C_{\rm m}$  estimate at the two potentials, both fittings showed a very high (R = 0.999) correlation with experimental curves. A good mono-exponential fitting correlation or a quasi-linear relation between  $ln(\Delta V_m)$  and time do not guarantee, along with the associated experimental noise, the Ohmicity of the tested RC and thus the independency of  $R_{\rm m}$  from  $V_{\rm m}$ . When the same voltage deflection was analyzed with the leastsquares algorithm (see Appendix) based on the non-Ohmic circuit (Fig. 7 B), the best-fitting solution corresponded to a  $C_{\rm m} = 193$  pF, which changed very little (mean  $\pm$  SE = 0.7) in all the analyzed traces from  $V_{\infty} = -1$  to  $V_{\infty} = -10$  mV.

### Effect of $C_{\rm m}$ size on the error in the estimate of $C_{\rm m}$ using the Ohmic assumption

The assumption of a constant  $R_{\rm m}$  for the cell membrane leads to errors in the estimate of  $C_{\rm m}$  as shown above. To investigate whether this error, described in Fig. 4 as a sigmoidal  $C_{\rm m}(\Delta V_{\rm m})$  function centered at the resting potential, depends

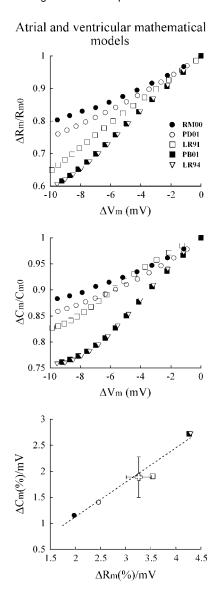


FIGURE 3 Voltage-dependency of  $R_{\rm m}$  and of the estimated  $C_{\rm m}$  in five mathematical models of cardiomyocytes. (Top)  $R_{\rm m}(\Delta V_{\rm m})$  as obtained through the CC protocol applied to the five mathematical models listed in Table 1. (Middle)  $C_{\rm m}(\Delta V_{\rm m})$  obtained with the same protocol. Results were normalized to the extrapolated resting values of  $R_{\rm m}$  ( $R_{\rm m0}$ ) and  $C_{\rm m}$  ( $C_{\rm m0}$ ), which were respectively set to 1 for comparison. (Bottom) The above traces were linearly fitted within the -10/0 mV  $\Delta V_{\rm m}$  range, to plot the slope of  $C_{\rm m}(\Delta V_{\rm m})$  versus the slope of  $R_{\rm m}(\Delta V_{\rm m})$  for the five models. The cross symbol represents the corresponding averaged estimate made on seven current-clamped rat ventricular myocytes ( $1.89\pm0.39~{\rm mV}^{-1}$  vs.  $3.26\pm0.25~{\rm mV}^{-1}$ ), also cited in the Results.

on the actual  $C_{\rm m}$  value of the cell, we performed simulations on a simple RC model including an experimentally derived parabolic  $R_{\rm m}(\Delta V_{\rm m})$ , and, in turn, three different values for  $C_{\rm m}$ . Simulated traces were fitted with mono-exponentials in the Ohmic assumption and measured  $C_{\rm m}(\Delta V_{\rm m})$  functions were reported as solid lines in Fig. 8, A and B. A typical non-Ohmic  $R_{\rm m}(\Delta V_{\rm m})$  function, like the one used here, led to a -11.8% (CC) and -2.4% (VC) errors in the estimate of  $C_{\rm m}$  at  $\Delta V_{\rm m}=-10$  mV in a 265 pF cell. When cell capacitance

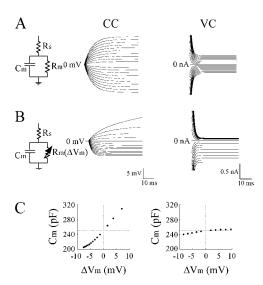


FIGURE 4 DC estimate of  $C_{\rm m}$  in Ohmic and non-Ohmic RC circuits. (A) Current-clamped (from -0.25 to 0.25 nA, step 0.025 nA) voltage displacements and voltage-clamped (from -20 to +20 mV, step 2 mV) current traces, mathematically simulated on the circuit reported on the left, with  $R_{\rm m}=56.5~{\rm M}\Omega$  and  $C_{\rm m}=250~{\rm pF}$ .  $R_{\rm s}$  was set to  $0~{\rm M}\Omega$  in CC and  $5~{\rm M}\Omega$  in VC. (B) Identical protocols simulated on the same circuit were  $R_{\rm m}(\Delta V_{\rm m})=56.5+4.8\times\Delta V_{\rm m}+0.17\times\Delta V_{\rm m}^2M\Omega$ . (C)  $C_{\rm m}$  versus  $\Delta V_{\rm m}$ , as calculated from mono-exponential fittings of the traces in B (solid circles).

was increased by 50%, this error decreased to -10.5% in CC and did not change in VC, whereas a 50% decrease of  $C_{\rm m}$  led to an increase of error up to -12.7% in CC and again no changes in VC. We then repeated the test for a series of  $C_{\rm m}$  from 5 to 1000 pF. Interestingly, we found that, as the cell capacitance increased, the error in  $C_{\rm m}$  estimate monotonically decreased from an initial value of 13.3% in CC, whereas it remained fairly constant at 2.8% in VC (with  $R_{\rm s}=5~{\rm M}\Omega$ ). When  $R_{\rm s}$  was increased to 20 M $\Omega$ , the error increased in VC up to 5.6% for a  $C_{\rm m}=5~{\rm pF}$ , and monotonically decreased to 4.2% for a  $C_{\rm m}=1000~{\rm pF}$ . To summarize, the percentage error in  $C_{\rm m}$  estimate decreases with the increasing of  $C_{\rm m}$ , being less important in voltage than in current clamp. The error in VC-estimate of  $C_{\rm m}$  depends on the uncompensated series resistance  $R_{\rm s}$ .

# Effect of the slope of $R_{\rm m}(\Delta V_{\rm m})$ function on the error in the estimate of $C_{\rm m}$ using the Ohmic assumption

We performed additional simulations to investigate how the slope of the  $R_{\rm m}(\Delta V_{\rm m})$  function affects the error in  $C_{\rm m}$  estimate. We chose three different  $R_{\rm m}(\Delta V_{\rm m})$  parabolic functions (Fig. 8 D) differing in the first-order coefficient (~ $\pm 50\%$  from a central value of 1.5) and all ranging within measured experimental values. We then run CC and VC simulations for an RC circuit including, in turn, the three  $R_{\rm m}(\Delta V_{\rm m})$  functions and having a  $C_{\rm m}=265$  pF (Fig. 8, E and E). With the increasing of the slope of the  $R_{\rm m}(\Delta V_{\rm m})$  function,

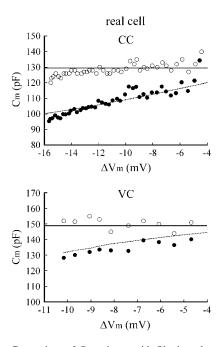
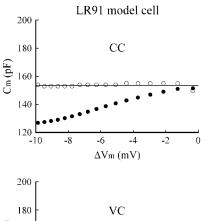


FIGURE 5 Comparison of  $C_{\rm m}$  estimate with Ohmic and non-Ohmic assumption in real ventricular myocytes.  $C_{\rm m}$ , first calculated through monoexponential fittings of CC-elicited voltage traces (top), and VC-elicited current traces (bottom), plotted as a function of  $\Delta V_{\rm m}$  (solid circles).  $C_{\rm m}$  is also reported as derived through the algorithm which assumes non-Ohmicity of the circuit (open circles). Solid line represents the average value of  $C_{\rm m}$  in the non-Ohmic assumption. This value, together with calculated  $R_{\rm s}$  and  $R_{\rm m}(\Delta V_{\rm m})$ , is incorporated in an equivalent circuit whose solutions, in CC and VC simulations, are fitted with mono-exponentials to derive  $C_{\rm m}$  for each  $\Delta V_{\rm m}$  (dotted lines).

the error in the estimate of  $C_{\rm m}$ , as measured at  $\Delta V_{\rm m}=-10$  mV, increased both in CC and VC from values of 4.4% and 0.7%, respectively (lower slope function) up to 22.4% and 7.5% (higher slope function).

### Good enough estimates of $C_{\rm m}$ with the Ohmic assumption

From the simulations performed on the non-Ohmic RC model in Fig. 4, it appears that the sigmoidal function of the estimated  $C_{\rm m}(\Delta V_{\rm m})$ , derived assuming a constant  $R_{\rm m}$ , has the property that it crosses the horizontal line corresponding to the actual value of  $C_{\rm m}$  in the resting membrane potential  $(\Delta V_{\rm m}=0)$ . Moreover the slope of this function is fairly constant in the  $V_{\rm m}$  range of interest (-10 mV <  $\Delta V_{\rm m}$  < 0 mV), where it can be approximated with a straight line. It follows that the proper value of cell capacitance could be, in principle, extrapolated with only two current injections (or VC pulses) experiments, using mono-exponential fittings, and ignoring therefore the voltage-dependency of  $R_{\rm m}$ . Histograms in Fig. 9 show, for both CC and VC, average estimates of  $C_{\rm m}$ , taken ignoring  $R_{\rm m}$  voltage-dependency and adopting mono-exponential fittings (first and second columns in each panel), deriving  $R_{\rm m}$  voltage-dependency and using the leastsquares fitting procedure (third column), or assuming the



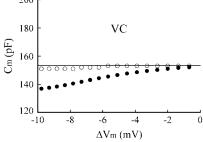
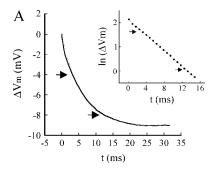


FIGURE 6 Comparison of  $C_{\rm m}$  estimate with Ohmic and non-Ohmic assumption in the LR91 model cell.  $C_{\rm m}$ , as calculated adopting the Ohmic assumption (*solid circles*) and the non-Ohmic assumption (*open circles*) through a CC and a VC protocol on the LR91 model. Horizontal lines represent the actual  $C_{\rm m}$  of the model. A series resistance of 10 M $\Omega$  was added in VC simulations.

function  $C_{\rm m}(\Delta V_{\rm m})$  to be linear and extrapolating the zero-potential value from two measures, taken approximately at  $\Delta V_{\rm m}=-10$  mV and  $\Delta V_{\rm m}=-5$  mV, for each cell (fourth column). The average value obtained with the extrapolation procedure does not significantly differ in CC and VC from the one measured with the non-Ohmic assumption.

### **DISCUSSION**

Among the several ways developed to measure  $C_{\rm m}$ , we focus the present study on the time-domain analysis of squarewave stimulations (as defined in Ref. 2) and the limitations we found in applying this technique to measure  $C_{\rm m}$  in single rat ventricular myocytes. The use, adopted within this approach, of the mono-exponential solutions 1 and 3 of Eq. 2 and Eq. 5 in a subthreshold  $V_{\rm m}$  range, coincides with the assumption that  $R_{\rm m}$  is constant in this range or, at least, its changes do not appreciably affect  $C_{\rm m}$  calculation. We show here that  $R_{\rm m}$  voltage-dependency around  $V_{\rm r}$  makes  $C_{\rm m}$  estimates, through the classical exponential fittings, also voltage-dependent, and that such dependency can be removed by using a mechanistic RC model that includes  $R_{\rm m}$ changes. As an alternative, a better estimate of  $C_{\rm m}$  can be extrapolated from at least two Ohmic measurements on the same cell. The finding of a voltage-dependency also when  $C_{\rm m}$  was measured in a very general model of the ventricular action potential like LR91, as well as in other more complex



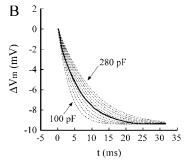


FIGURE 7 Ohmic and non-Ohmic analysis of a current-clamped voltage deflection. (A) Mono-exponential fitting (dotted line) ( $\tau=5.7$  ms) of a current-clamped (-0.24 nA) voltage displacement (solid line) from a ventricular myocyte. (Inset) Linear fitting (dotted line) of the logarithm of  $\Delta V_{\rm m}$  (solid circles; only one in every four experimental samples is plotted). (B) Dotted lines are solutions of Eq. 2 with  $R_{\rm m}(\Delta V_{\rm m})=9.7+2.7 \times \Delta V_{\rm m}+0.06\times \Delta V_{\rm m}^2\,M\Omega$ , experimentally derived from the same cell, and for  $C_{\rm m}$  values from 100 pF to 280 pF (only 1 in every 20 solutions is reported); solid line is the experimental voltage deflection.

mathematical models, rules out the possibility that such effect could be, even only partially, due to experimental artifacts like time- or voltage-changes in  $R_s$  or changes in experimental parameters other than those  $(R_m, C_m, R_s)$  included in the simple representation of Fig. 4 B.

It should be noted that a frequently adopted variant of constant step VC protocol to measure  $C_{\rm m}$  is the one (see Materials and Methods) based on the calculation of the charge underlying the capacitive current transient. An earlier version of this approach simply calculated  $C_{\rm m}$  as in Eq. 6. Such calculation is not accurate and has been more recently replaced by Eq. 7, where the mono-exponentially derived time constant  $\tau$  appears explicitly, and therefore makes this protocol suffer as well from the voltage-dependency of  $R_{\rm m}$ . Indeed, errors in  $C_{\rm m}$  calculations using Eq. 7 have been derived for the voltage-clamp simulation reported in Fig. 4 B without finding any difference from those derived with the classical protocol (data omitted for the sake of clarity). Therefore we did not discuss in a separate section errors in  $C_{\rm m}$  estimate derived with the numerical integration of the current transient during voltage steps.

### Limits of the Ohmic assumption

 $R_{\rm m}$  voltage-dependency for subthreshold potentials is known in cardiac tissue at a cellular level (13,27), and has a part in

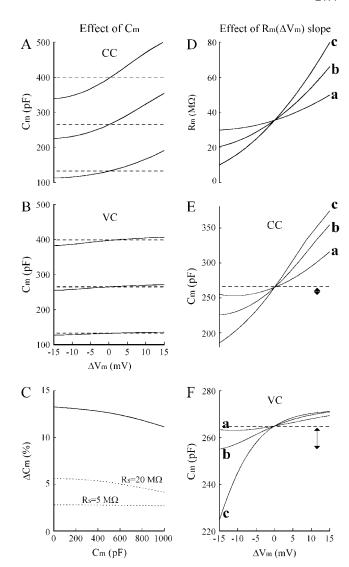
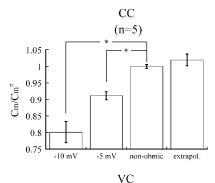


FIGURE 8 Effect of  $C_{\rm m}$  and  $R_{\rm m}(\Delta V_{\rm m})$ -slope on the accuracy of  $C_{\rm m}$  estimate in a simple RC circuit. (A and B) CC and VC estimate of  $C_{\rm m}$  through Ohmic assumption on an RC model including an  $R_{\rm m}(\Delta V_{\rm m})=35.5+1.5\times\Delta V_{\rm m}+0.034\times\Delta V_{\rm m}^2M\Omega$  and an  $R_{\rm s}=5$  M $\Omega$  (in VC), for three different values of  $C_{\rm m}$  (horizontal dotted lines). (C) Error in  $C_{\rm m}$  estimate (percent underestimate from the actual  $C_{\rm m}$ ), as measured at  $\Delta V_{\rm m}=-10$  mV, for different values of  $C_{\rm m}$ , in CC (solid line) and VC (dotted lines) simulated tests, and for two values of  $R_{\rm s}$ . (D) Three  $R_{\rm m}(\Delta V_{\rm m})$  parabolic functions differing for the slope. (E and F) CC and VC estimates of  $C_{\rm m}$  by Ohmic assumption on an RC model including, in turn, the three functions. The double-arrow symbols represent the typical experimental noise level in  $C_{\rm m}$  estimate.

explaining subthreshold behavior of extracellular membrane polarization (29). We limited the majority of our experimental work and analysis on  $R_{\rm m}$  changes in the  $\sim 10$  mV hyperpolarized  $V_{\rm m}$ -range of well polarized ( $V_{\rm r}=-73.45\pm0.69$  mV) rat left-ventricular cells (n=24). With this, we deliberately wanted to avoid eliciting the time-dependent processes that develop in cardiac membrane for depolarizing potentials (e.g., activation of inward sodium current, inward L-type calcium current, calcium-independent transient outward



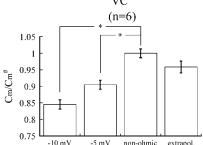


FIGURE 9 Histograms comparing CC and VC estimate of  $C_{\rm m}$  with Ohmic and non-Ohmic assumption in real ventricular myocytes. (First and second bars) Estimate made through the Ohmic assumption at  $\Delta V_{\rm m}=-10$  mV and  $\Delta V_{\rm m}=-5$  mV, respectively. (Third bar) Estimate made through the non-Ohmic assumption ( $C_{\rm m}^{\rm th}$ ). (Fourth bar) Estimate made through extrapolation from pairs of Ohmic-assumption measurements. All bars are normalized to third bar, which is set to 1 (the asterisk symbol indicates significant differences).

potassium current, steady-state outward potassium current; Ref. 30) and for more hyperpolarized potentials (e.g.,  $I_{\rm K1}$  time-dependent block and  $I_{\rm f}$  activation; Ref. 31). In fact, voltage traces always reached a plateau within CC steps, as well as current traces never showed time-dependent components other than the capacitive peak during VC steps on tested ventricular myocytes.

The 40–50% decrease of  $R_{\rm m}$  when membrane potential was current- or voltage-clamped from  $V_r$  to  $(V_r-10)$  mV (see Fig. 1) is reflected into the progressive compression/broadening of the elicited voltage/current traces. In the case of the mathematical LR91 model, the 40% decrease of  $R_{\rm m}$  for  $\Delta V_{\rm m} = -10$  mV, corresponds to a 72% increment of  $g_{\rm K1}$ whereas other ionic conductances included in the model do not change (carried simulations not shown). Indeed, this is also the case for the other more complex mathematical models, where, in this subthreshold region, the I-V relationship with the highest degree of nonlinearity is that of  $I_{K1}$  which, moreover, overwhelms all the others in absolute intensity. In fact, the simple analysis of published steady-state  $I_{K1}$ -V curves recorded in rat and other mammals ventricular myocytes (e.g., Refs. 32–35) shows that  $I_{K1}$  starts rectifying at potentials that are at least 10- or 15-mV hyperpolarized, with respect to the typical  $V_r$  for this cell type, which has to be reflected in some  $R_{\rm m}$  voltage-dependency. From our simulation work, we can rule out the direct contribution to

 $R_{\rm m}$  rectification of the electrogenic sodium-potassium pump, whose I-V relationship is linear in the subthreshold region of interest of this study (see, for example,  $I_{NaK}$  equations in PD01, LR94, RM00, and Ref. 36). For the same reason, we can exclude calcium, sodium, and potassium background currents which, although flowing in this voltage range, are usually formulated as linear leakage currents therefore not possibly contributing directly to any  $R_{\rm m}$  rectification (see, for example, related equations in PD01 and LR94). It is tempting to hypothesize a significant role of the sodiumcalcium exchanger current, whose IV relationship slightly deviates from linearity in the same region (30,37), but this would need further mathematical and experimental work to be confirmed and quantified. Furthermore, it is possible that some other rectifying mechanisms would be present that are still not included in the models and, therefore, in our knowledge of membrane electrical properties.

A major point of the present work is to show that the measure of  $C_{\rm m}$  within the Ohmic assumption is voltage-dependent in a non-negligible manner. Indeed such dependency was always present in tested ventricular myocytes (Figs. 2 and 5), being less dramatic in VC than in CC, and only slightly depending on the actual value of  $C_{\rm m}$  (see experiment in Fig. 8). In this regard, it is interesting to note the 26-pF difference, reported by Tseng and co-authors in canine ventricular myocytes, between average  $C_{\rm m}$  estimates when measurements were performed in CC (voltage displacements up to -10 mV) and VC (-5 or -10 mV steps) by microelectrode impalement (38). According to our findings, both values underestimate the actual  $C_{\rm m}$ , being the CC error at 54 pF worst than the VC error at 80 pF.

A voltage-dependency in the estimate of  $C_{\rm m}$  can actually become hard to detect and therefore negligible, for example, in hyperkalemic conditions where  $I_{K1}$ -V curve shifts horizontally toward depolarized potentials and vertically toward more positive currents, becoming therefore more linear around its reversal potential (see  $[K^+]_0$ -dependency of  $I_{K1}$ equation in Ref. 33, and in Ref. 30). The same  $[K^+]_0$ dependency can be viewed in the total steady-state I-V relationship (e.g., Ref. 38). When [K<sup>+</sup>]<sub>0</sub> increases, the slope of  $R_{\rm m}(\Delta V_{\rm m})$  function becomes smaller and errors in the estimate of  $C_{\rm m}$  will be negligible compared with experimental noise. If we consider, for example, the experiment in Fig. 8 D, a cardiac myocyte with an  $R_{\rm m}(\Delta V_{\rm m})$  function a, characterized by a very weak voltage-dependency, will bring about, when analyzed in VC through the Ohmic assumption (Fig. 8 F), an underestimate of  $C_{\rm m}$ , as measured at  $\Delta V_{\rm m}$ = -10 mV, < 1%, which will be masked within the typical noise level ( $\sim$ 5–6%) of our experiments. On the other hand, an increase in series resistance, especially in cells with higher  $R_{\rm m}(\Delta V_{\rm m})$  slope, can produce appreciable differences also in VC, whereas in CC, differences are always measurable practically in all physiological conditions. This is noteworthy, particularly if we consider that, although the great majority of recent cardiac cellular electrophysiological studies

adopts VC constant pulses to measure  $C_{\rm m}$  (e.g., Refs. 39 and 40), many still use the CC approach (21,22), which will then lead to much larger errors.

 $C_{\rm m}$  measurements within homogeneous cell populations suffer frequently for a consistent dispersion (SD often up to 50% of the average) which could be attenuated with the non-Ohmic assumption, allowing better resolution of  $C_{\rm m}$  changes following different pathological conditions or pharmacological treatments. Moreover, errors in  $C_{\rm m}$  evaluation can complicate calculations on intracellular ion dynamics. For example a 10% underestimate of  $C_{\rm m}$  (pF) leads to an 11% overestimate of current density (pA/pF), a 4% underestimate of cell volume in rat ventricular cardiomyocyte (23), and therefore an analogous overestimate of intracellular ion concentration changes. Cell volume and intracellular ion concentration changes will be further underestimated (up to 10%) in species like rabbit, where volume/surface relation is steeper (23).

The correlation, found in the four ventricular models and the one atrial model analyzed, between the slope of the relative error in  $C_{\rm m}$  estimate and the slope of  $R_{\rm m}(\Delta V_{\rm m})$  (Fig. 3, bottom panel), furthermore emphasizes the generality of the principle: the input resistance of resting cardiomyocytes rectifies in the subthreshold voltage range under study, and such rectification brings about a proportional error in  $C_{\rm m}$ estimate. This proportionality is fully satisfied by our experimental data, as shown by their position on the correlation line of Fig. 3 (bottom panel). Interesting to note is the failure of the PD01 model to exactly reproduce rat data in this correlation plot, most likely due to the particular  $I_{K1}$  equation chosen in the original work (30), where, on the other hand, the authors themselves recognize the nonuniform properties of  $I_{K1}$  across the ventricle as one of the potential limitations of their mathematical description (see also Ref. 41).

### A mechanistic non-Ohmic assumption

We call the model described in Fig. 4 B "mechanistic" because it is based only on properties of an experimental observable  $(R_{\rm m})$ , independently on its biological determinants (ion channels, pumps, exchangers, etc.). This simple model shows that the property of  $R_{\rm m}$  to vary parabolically with  $V_{\rm m}$  is enough, by itself, to qualitatively explain voltage and current asymmetry in response to symmetric current-/ voltage-clamp protocols. It also accounts for the voltagedependency of  $C_{\rm m}$  estimate in vivo and in the mathematical model cells. Finally it shows that, even though monoexponential functions fit quite well the solutions of Eq. 2 and Eq. 5 for the non-Ohmic circuit, nevertheless they are solutions of a wrong model of the cell electrical properties and they lead therefore to wrong  $C_{\rm m}$  estimates. If, instead, numerical solutions of Eq. 2 and Eq. 5 including the  $R_{\rm m}(\Delta V_{\rm m})$ relation are used, the  $C_{\rm m}$  measure becomes independent from  $V_{\rm m}$  and gives estimates that are only a little dispersed around a mean value (Fig. 5), as can also be appreciated in the cell model simulations (e.g., Fig. 6). A further validation of the consistency of the least-square algorithm (see Appendix) to measure  $C_{\rm m}$  comes from the experiment in Fig. 5. A mechanistic mathematical model of a real rat ventricular myocyte, built with experimentally derived  $R_{\rm m}(\Delta V_{\rm m})$ ,  $R_{\rm s}$ , and a constant  $C_{\rm m}$  calculated with the least-square protocol on the same cell, was challenged with CC and VC constant steps and analyzed in terms of mono-exponentials. The fact that the resulting  $C_{\rm m}$  values fit well those derived with the Ohmic assumption on the real cell, demonstrates that the voltage-dependency of  $R_{\rm m}$  is enough to explain the error in  $C_{\rm m}$  estimate, and no other effects like leaky seals, additional uncompensated stray capacitances, series resistances, or different equivalent circuits (11), in principle, need to be considered.

It could be argued that the least-square algorithm presented in this study as a tool to calculate  $C_{\rm m}$  in a voltageindependent manner is too complicated and demanding, especially for what concerns off-line numerical processing of the data, making it therefore not suitable for the general purpose of monitoring passive electrical properties, which is often ancillary in most cardiac cellular electrophysiological studies. To answer this concern, we propose a procedure where an algebraic property of the  $C_{\rm m}$  calculation with the Ohmic assumption is used to extrapolate the real value of  $C_{\rm m}$ without need of any further experimental or mathematical work, as summarized in Fig. 9. Some authors use protocols where symmetrical (depolarizing and hyperpolarizing) VC steps are imposed to the membrane and  $C_{\rm m}$  averaged from the analysis of the two opposite current transients (e.g., Ref. 15). It should be noted that this procedure is quite different from the one we are suggesting here and can also lead to misestimate of  $C_{\rm m}$ , because  $C_{\rm m}$  error in the Ohmic assumption is not symmetrical with respect to  $V_r$  (see curve c in Fig. 8 F).

### Why VC gives a better C<sub>m</sub> estimate

The typical first-order linear differential equation generating mono-exponential functions as solutions is of the type

$$\dot{\mathbf{y}}(t) = a - b \times \mathbf{y}(t),\tag{8}$$

where a and b are constants. This is, for example, the form of Eq. 2 of CC in the Ohmic case when  $R_{\rm m}$  is constant. Conversely, when  $R_{\rm m}$  becomes a function of  $V_{\rm m}$ , Eq. 2 assumes a qualitatively different form, whose solutions will always deviate from mono-exponentials as much as  $R_{\rm m}$  is voltage-dependent.

In the case of Eq. 5 of VC, this can be conveniently rewritten as

$$\dot{V}_{\rm m}(t) = \frac{V_{\rm c}}{C_{\rm m} \times R_{\rm s}} - \frac{V_{\rm m}(t)}{C_{\rm m} \times R_{\rm s}} \left(1 + \frac{R_{\rm s}}{R_{\rm m}(V_{\rm m})}\right),\tag{9}$$

where it becomes evident that the linear form of Eq. 8 tends to be restored when  $R_{\rm m}\gg R_{\rm s}$ .

This explains qualitatively why, assuming the same voltage-dependency of  $R_{\rm m}$ , VC-derived current traces deviate less from mono-exponentials than CC-derived voltage displacements. In other words, provided  $R_{\rm s}$  is kept much lower than  $R_{\rm m}$ , VC gives best estimates of  $C_{\rm m}$ , as we demonstrated in this study with both experimental and numerical approaches.

### Limitations of the study

A limitation of this work is that, although the very general mechanism of subthreshold  $R_{\rm m}$  rectification is presented with its implications on  $C_{\rm m}$  estimate, the relative role of the ionic mechanisms underlying this property have not been unambiguously defined in vivo nor in silico. Although, as in previous studies (26,27), a primary contribution of  $I_{K1}$  is strongly suggested, additional experimental and numerical work will help to better define the possible role of sodiumcalcium exchanger or other ionic mechanisms in  $R_{\rm m}$  rectification. Also, we do not report here on any intervention made to modify the different ionic mechanisms of  $R_{\rm m}$ voltage-dependency. Work in this direction will be required, for example, to investigate whether there are conditions where the membrane of resting cardiomyocytes behaves Ohmically, helping to better explain its subthreshold electrical properties in physiological and pathological states.

### **CONCLUSIONS**

This study emphasizes that attention should be paid to the subthreshold voltage-dependency of  $R_{\rm m}$  if  $C_{\rm m}$  is to be measured with classical DC protocols. Large errors always arise from the CC approach, but VC can also be substantially affected. Accurate measures can be achieved by taking  $R_{\rm m}$  ( $\Delta V_{\rm m}$ ) into account in the analysis of CC and VC experimental results or by ignoring this voltage-dependency, and extrapolating results obtained from at least two different  $\Delta V_{\rm m}$  values to  $\Delta V_{\rm m}=0$ .

It is straightforward to hypothesize that the voltage-dependency of  $R_{\rm m}$  would also play a role in other techniques to measure  $C_{\rm m}$ , especially those based on complex impedance analysis, widely adopted in the literature and based on the AC study of the same Eq. 2 and Eq. 5.

### **APPENDIX**

The non-Ohmic form of Eq. 2 and Eq. 5 includes an  $R_{\rm m}$  which is not a constant, but is, instead, a function of the membrane potential. Whatever this function (we used second-order polynomials from experimental fittings in this work), it is not possible to find explicitly the solutions for these new equations, which we should solve numerically.

### Fitting procedure with the non-Ohmic solutions

### Current-clamp

A set of traces like those in Fig. 1 A was fitted with mono-exponentials to derive the parabolic functions  $R_{\rm m}(\Delta V_{\rm m})$  and  $C_{\rm m}(\Delta V_{\rm m})$ .  $R_{\rm m}(\Delta V_{\rm m})$  was

replaced into Eq. 2, which was then solved numerically for each current  $i_p$ , for all the  $C_{\rm m}$  values of an n-long vector  $\hat{C}_{\rm m} = [C_{\rm m,1}, C_{\rm m,2}, C_{\rm m,3}, \ldots, C_{\rm m,n}]$ , where  $C_{\rm m,n}$  and  $C_{\rm m,1}$  were, respectively, the central value of the derived  $C_{\rm m}$  range  $\pm$  50 pF. In the case of the experiment shown in Fig. 5, for example, the non-Ohmic form of Eq. 2 was solved for 42  $i_p$  values and, for each  $i_p$ , 100 times for  $C_{\rm m}$  values from 65 to 165 pF. For each current injection, the sum of the squared-errors between the numerically integrated solutions and the experimental vector was calculated n times to obtain an n-long vector LS. The actual  $C_{\rm m}$  was then derived as the element of  $\hat{C}_{\rm m}$  that minimizes LS (least-squares method). An example of this procedure is reported in Fig. 7 B.

### Voltage-clamp

Same approach as in current-clamp, where Eq. 5 was solved for a given set of voltage steps  $V_{\rm c}$  and, for each voltage-clamped  $V_{\rm c}$ , for all the elements of the vector  $\hat{C}_{\rm m}$ .

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